



Anisotropy From basics to 3D modeling

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Thanks to collaborators of my MT working group

Michael Häuserer (Rwenzori, Uganda) Alexander Löwer (Rhenish Massif, Germany) Marcel Cembrowski (Pyrenees, Spain) Lourdes Gonzales (Tierra del Fuego, Argentina) Philip Hering (Ceboruco, Mexico) Ying Liu (Western Junggar, China) Colin Hogg (Sao Miguel, Azores) Sharare Zhian (Zagros, Iran) César Castro (Tepic-Zacoalco, Mexico)





Content for today:

- Motivation why anisotropy rather than isotropy?
- Numerical simulations in 3D
- The real world





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Starting with a numerical simulation **3D inversion (ModEM)** of simulated data (full impedance tensor and tipper) for 6 periods between 1 – 100 s at 441 sites equally distributed in 20 km x 20 km

(Löwer&Junge, PAGEOPH 2017 (online))







According to Occam's Principle, what model do you prefer?





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3D Model Study



 ho_a anisotropic: $ho_1=1000~\Omega m$ $ho_2=10~\Omega m$

 $\rho_n = 100 \ \Omega m$

10 sec

 $\rho_a = 10 \ \Omega m$

Apparent resistivity



10 sec

 $\rho_a = 10 \ \Omega m$

Apparent resistivity



10 sec

 $\rho_a = 10 \ \Omega m$

Phase



Resistor isotropic

10 sec

$\rho_a = 1000 \ \Omega m$

Apparent resistivity



Resistor isotropic

10 sec

 $\rho_a = 1000 \ \Omega m$

Phase



10 sec

 $\rho_a = 10 \ \Omega m$

Apparent resistivity









10 sec

 $\rho_a = 10 \ \Omega m$

Phase









Some MT Definitions

Impedance Tensor
$$\mu \mathbf{Z}$$
:
 $\begin{pmatrix} E_x \\ E_y \end{pmatrix} = \begin{pmatrix} Z_{xx} & Z_{xy} \\ Z_{yx} & Z_{yy} \end{pmatrix} \begin{pmatrix} B_x \\ B_y \end{pmatrix}$ or $\underline{E} = \mathbf{Z}\underline{B}$
Apparent Resistivity ρ_a : $\rho_{a,xy} = \frac{\mu}{\omega} |Z_{xy}|^2$, Phase: $\varphi_{xy} = \tan^{-1} \left(\frac{\Im Z_{xy}}{\Re Z_{xy}} \right)$

Phase Tensor
$$\mathbf{\Phi}$$
: $\boldsymbol{\phi} = (\Re Z)^{-1}(\Im Z)$ (Caldwell et al., 2004)

Apparent Resistivity Tensor ρ : $\rho = (i\mu/\omega)det(Z)Z(Z^{-1})^T$ (Brown, JGR 2017)

Apparent Current Density \underline{J} : $\underline{E} = \rho \underline{J}$ (Brown, JGR 2017)



Phase Tensor Φ : $\phi = (\Re Z)^{-1}(\Im Z)$ (Caldwell et al., 2004)

Apparent Resistivity Tensor ρ : $\rho = (i\mu/\omega)det(Z)Z(Z^{-1})^T$ (Brown, JGR 2017) $\rho = U_a + iV_a$ $\phi_a = (U_a)^{-1}(V_a)$



Phase Tensor $\mathbf{\Phi}$:



Apparent Resistivity Tensor ρ : $\rho = ({}^{i\mu}/_{\omega})det(Z)Z(Z^{-1})^T$ (Brown, JGR 2017) $\rho = U_a + iV_a$ $\phi_a = (U_a)^{-1}(V_a)$



Phase Tensor Φ : $\phi = (\Re Z)^{-1} (\Im Z)$ (Caldwell et al., 2004)

Apparent Resistivity Tensor ρ : $\rho = (i\mu/\omega)det(Z)Z(Z^{-1})^T$ (Brown, JGR 2017) $\rho = U_a + iV_a$ $\phi_a = (U_a)^{-1}(V_a)$

In general for 1D subsurface:

Behaviour of B and E with depth and period

$$\begin{pmatrix} E_x \\ E_y \end{pmatrix} = \begin{pmatrix} 0 & Z_{xy} \\ Z_{yx} & 0 \end{pmatrix} \begin{pmatrix} B_x \\ B_y \end{pmatrix}$$

$$\rho_{axy} = \rho_{ayx}$$

$$\varphi_{xy} = \varphi_{yx} + \pi$$

$$B_{y}(z) = B_{y0}e^{-\sqrt{i\frac{\mu_{0}}{\rho}\omega}z}$$

$$Z_{xy} = \frac{E_x}{B_y}$$
$$E_x = (1+i) \sqrt{\frac{\rho\omega}{2\mu_0}} B_y$$



Azimuthal anisotropic Conductivity

Generally
$$\boldsymbol{\sigma} = \begin{pmatrix} \sigma_{xx} & \sigma_{xy} & 0\\ \sigma_{xy} & \sigma_{yy} & 0\\ 0 & 0 & \sigma_3 \end{pmatrix} = \boldsymbol{R}_{\alpha}^T \boldsymbol{\sigma}' \boldsymbol{R}_{\alpha}$$

Ohm's law

$$J_{x} = \sigma_{xx}E_{x} + \sigma_{xy}E_{y}$$
$$J_{y} = \sigma_{xy}E_{x} + \sigma_{yy}E_{y}$$

$$\rightarrow \underline{J} \not\parallel \underline{E}$$



Behaviour of B and E with depth and period

Anisotropic homogeneous halfspace, $\alpha = 0^{\circ}$



Behaviour of B and E with depth and period

Anisotropic homogeneous halfspace, $\alpha = 90^{\circ}$



Behaviour of B and E with depth and period

Anisotropic homogeneous halfspace, $\alpha = 30^{\circ}$



Behaviour of B, E and J with depth and period Isotropic



Behaviour of B, E and J with depth and period

Isotropic, Anisotropic Layer, α = -20°



x-axis y-axis

Behaviour of B, E and J with depth and period

Isotropic, Anisotropic Layer, α = -20°



(Hering et al., 2018)



y-axis

(a)
3D isotropic - anisotropic: What happens inside the body?

<u>3 Studies:</u>

- Anisotropic Cube within isotropic half space
- Isotropic Cube above anisotropic half space
- Dipping Anisotropy

Anisotropic Cube within isotropic half space



Transfer functions: phase tensor, app.res. tensor

plane view, period 10 sec

Phasetensor, 20d, 10 s 50 40 70 30 60 20 50 x [km] 40 -10 -20 - 30 -30 20 -40 -50 -40 20 30 40 50 -50 -30 -10 0 10 y [km]





Transfer functions: phase tensor, app.res. tensor

plane view, period 10 sec

 $\Im
ho$







Transfer functions: apparent resistivity, phase and tipper

tz, rhoayx, 20d, 10 s tz, phiyx, 20d, 10 s 2.2 65 50 50 40 40 60 2.1 1 30 30 55 20 20 2 0.2 0.2 50 10 10 x [km] x [km] 0 1.9 0 45 -10 -10 40 1.8 0 0 -20 -20 35 -30 -30 30 -40 J(HxPol), JzR, 20e, 10 s, 6 km 50 0.06 -50 25 40 0 50 -50 0 y [km] y [km] 30 0.04 20 0.02 10 $\rho_1 = \underset{\mathsf{X}}{100} \, \Omega m$ x [km] 0 0 $\rho_2 = 10 \,\Omega m$ -10 -0.02 0 -20 **Current density** $\gamma = 30^{\circ}$ -0.04 -30 within the cube -40 -0.06 -50 0 50 -50 y [km] z

plane view, period 10 sec

Transfer functions: apparent resistivity, phase and tipper

tz, rhoayx, 20d, 10 s tz, phiyx, 20d, 10 s 2.2 65 50 50 40 40 60 2.1 1 30 30 55 20 20 2 0.2 0.2 50 10 10 x [km] x [km] 0 0 1.9 45 -10 -10 40 1.8 Lο 0 -20 -20 35 -30 -30 30 -40 J(HxPol), JzR, 20e, 10 s, 4 km 50 0.06 -50 25 40 -50 0 0 50 y [km] y [km] 30 0.04 20 0.02 0.4 10 $\rho_1 = \underset{\mathsf{x}}{100} \,\Omega m$ [km] 0 0 × $\rho_2 = 10 \,\Omega m$ -10 -0.02 $\perp 0$ -20 **Current density** $\gamma = 30^{\circ}$ -0.04 -30 above the cube -40 -0.06 -50 -50 0 50 y [km] z

plane view, period 10 sec







Figure1-20e Figure2-20e Figure3-20e Figure4-20e Figure5-20e Figure6-20e Figure7-20e Figure8-20e Figure9-20e Figure10-20e Figure11-20e Figure11-20e Figure10-20e Figure



Phase Tensor, Tipper







 $\rho_1 = 100 \ \Omega m$

 $\gamma = 30^{\circ}$

Ζ



Current Density



Phase Tensor, Tipper







Figure1-20e Figure2-20e Figure3-20e Figure3-20e





Phase Tensor, Tipper











Phase Tensor, Tipper



How can we explain the rotation of the field vectors?

Downward – Upward Propagating Wave



Isotropic Cube above anisotropic half space



Isotropic Cube above anisotropic half space



Isotropic cube above anisotropic half space



Isotropic cube above anisotropic half space



Isotropic cube above anisotropic half space



Transfer functions: phase tensor, app.res. tensor

plane view, period 10 sec

 ϕ

 $\Re \rho$



Transfer functions: phase tensor, app.res. tensor

plane view, period 10 sec

 $\Im \rho$

 $\Re \rho$



Dipping Anisotropy



1D isotropic - anisotropic: What happens inside the body?



Transfer functions: Apparent Resistivity, Phase, Tipper plane view, period 10 sec

 $\rho_{a,yx}$

 φ_{yx}



Transfer functions: phase tensor, app.res. tensor

plane view, period 10 sec

 $\rho_{a,yx}$

 φ_{yx}

Comparison: Isotropic Cube



Transfer functions: Apparent Resistivity, Phase, Tipper

plane view, period 10 sec

 $\rho_{a,yx}$

 φ_{yx}



Transfer functions: phase tensor, app.res. tensorplane view, period 10 sec ϕ $\Re \rho$



Transfer functions: phase tensor, app.res. tensor plane view, period 10 sec



 $\Re \rho$







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 - Case 1: African Rift (Häuser&Junge, GJI 2011)
 - Case 2: Tierra del Fuego (Gonzales et al., Nat.Sci.Rep. 2019)
 - Case 3: Ceboruco (Hering, Diss. 2019)

Case Study 1: East African Rift

Electrical mantle anisotropy and crustal conductor: a 3-D conductivity model of the Rwenzori Region in western Uganda

Häuserer, M. and Junge, A., GJI 2011



















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Case Study 2: Tierra Del Fuego

Mantle flow and deep electrical anisotropy in a main gateway: MT study in Tierra del Fuego Gonzales et al., Nat.Sci.Rep. 2019



Case Study 2: Tierra Del Fuego

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Isotropic inversion (ModEM)

Ying et al., JGR 2019

Observations

Case study







Compared to isotropic dyke models with unrealistic high resisitivity contrast

Bulk Anisotropy yields realistic moderate resistivities





Conclusions

- Indications for anisotropic conductivity in crust and mantle
- Magnetotelluric is the (only?) method to detect deep electrical anisotropy
- Array site distribution necessary
- Preferable observables: Complex Resistivity Tensor and Tipper (Brown, JGR 2017, Hering et al., JGR 2019)
- Comparison with seismic anisotropy (spatial pattern)
- Important parameter for understanding geodynamic processes

Thank you for your attention